



Núcleo de Economia Regional e Urbana da Universidade de São Paulo The University of São Paulo Regional and Urban Economics Lab





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## Ejercicio Práctico de Aplicación

*Comisión Nacional de Prevención de Riesgos y Atención de Emergencias – Desarrollo Estratégico del SNGR San José, Costa Rica, 2-3 de junio, 2022* 

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## Input-output table



The input-output table is basically an accounting system – a double entry one similar to that prepared for a business in which sales and purchases or assets and liabilities will be shown but, in this case, for an economy.

The next step is to **prepare an economic model** so that we can trace the impact of changes in one sector on the rest of the economy.

We do this because the nature of interdependence among sectors varies.

### **Key assumptions**

We assume that each sector produces goods and services according to a fixed recipe (formally known as a **production function**)

$$a_{ij} = \frac{z_{ij}}{x_j} \quad \forall \quad i,j = 1, 2, \dots, n$$

- Fixed technical coefficient
- Constant returns to scale
- Sectors use inputs in fixed proportions

## **Production function**



FIGURE 2-1 Production functions in input space.

### **Key assumptions**

Inputs are expressed in monetary terms since it would be difficult to combine tons of iron ore with megawatts of electricity, or hours of labor in some consistent fashion.

This fixed recipe enables us to express the transactions in proportional form, also known as *direct coefficients*.

### **Key assumptions**

The final assumption is that the **economy is driven by signals emanating from final demand** (consumers, government, exports); this is the *exogenous* part of the economy, while the interindustry transactions respond to these signals and are therefore *endogenous*.

### **Basic relations**

$$\sum_{j=1}^{n} z_{ij} + y_i \equiv x_i \quad \forall \ i, j = 1, 2, \dots, n$$

 $z_{ij}$  = flows of intermediate consumption from sector *i* to sector *j*  $y_i$  = final demand of sector *i*  $x_i$  = total supply of sector *i* 

### **Basic relations**

Replacing  $a_{ij} = \frac{z_{ij}}{x_j}$  in the previous equation, we have:

$$\sum_{j=1}^{n} a_{ij} x_j + y_i = x_i \quad \forall \ i, j = 1, 2, ..., n$$

$$Ax + y = x$$
$$x = (I - A)^{-1}y$$
$$B = (I - A)^{-1}$$

- **A** = matrix of technical direct coefficients
- **B** = Leontief inverse matrix

### **Basic relations**

The Leontief inverse matrix **B** shows the coefficients (economic multipliers) that measure the successive effects on the economy as a result of the initial increase in production of an economic activity branch:

$$x = (\mathbf{I} - \mathbf{A})^{-1} y$$

$$\begin{bmatrix} x_1 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} b_{11} & \cdots & b_{1n} \\ \vdots & \ddots & \vdots \\ b_{n1} & \cdots & b_{nn} \end{bmatrix} \begin{bmatrix} y_1 \\ \vdots \\ y_n \end{bmatrix} = \begin{bmatrix} b_{11}y_1 & \cdots & b_{1n}y_n \\ \vdots & \ddots & \vdots \\ b_{n1}y_1 & \cdots & b_{nn}y_n \end{bmatrix}$$

The entries reveal the direct and indirect impacts on a sector when final demand in the sector at the top of the column changes by \$1 (or \$1 million or \$100 million). The sum of the elements in a column generate the **output multipliers**.

### Calculation of the output multiplier (backward linkages)

$$o_j = \sum_{i=1}^n b_{ij}$$
,  $i, j = 1, ..., n$ 

### **Decomposition of the output multiplier**

- **Total effect:**  $ET_j = o_j$
- **Indirect effect:**  $EID_j = o_j \sum_i a_{ij} 1$
- **Direct effect:**  $ED_j = \sum_i a_{ij}$

**Initial effect:**  $EI_j = 1$ 

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|                                    | Buying Sectors<br>Region L | Buying Sectors<br>Region M |          |          |         |
|------------------------------------|----------------------------|----------------------------|----------|----------|---------|
| Selling sectors<br><b>Region L</b> | Interindustry Inputs       | Interindustry Inputs<br>LM | FD<br>LL | FD<br>LM | TO<br>L |
| Selling sectors <b>Region M</b>    | Interindustry Inputs<br>ML | Interindustry Inputs       | FD<br>ML | FD<br>MM | TO<br>M |
|                                    | Imports from the World     | Imports from the World     | Μ        | М        | М       |
|                                    | Sales Taxes                | Sales Taxes                | т        | т        | т       |
|                                    | Value Added                | Value Added                |          |          |         |
|                                    | Total Output L             | Total Output M             |          |          |         |

## Interregional IO models



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### **Interregional model**

$$A = \begin{bmatrix} A^{LL} & \vdots & A^{LM} \\ \cdots & \cdots & \cdots \\ A^{ML} & \vdots & A^{MM} \end{bmatrix} \quad y = \begin{bmatrix} y^L \\ \cdots \\ y^M \end{bmatrix} \quad x = \begin{bmatrix} x^L \\ \cdots \\ x^M \end{bmatrix}$$
$$\left\{ \begin{bmatrix} I & \vdots & 0 \\ \cdots & \cdots \\ 0 & \vdots & I \end{bmatrix} - \begin{bmatrix} A^{LL} & \vdots & A^{LM} \\ \cdots & \cdots & \cdots \\ A^{ML} & \vdots & A^{MM} \end{bmatrix} \right\} \begin{bmatrix} x^L \\ \cdots \\ x^M \end{bmatrix} = \begin{bmatrix} y^L \\ \cdots \\ y^M \end{bmatrix}$$
$$(I - A)x = y \quad \longrightarrow \quad x = (I - A)^{-1}y$$

### Multipliers in interregional IO models

$$A = \begin{bmatrix} A^{LL} & A^{LM} \\ A^{ML} & A^{MM} \end{bmatrix} \rightarrow B = (I - A)^{-1} = \begin{bmatrix} B^{LL} & B^{LM} \\ B^{ML} & B^{MM} \end{bmatrix}$$

Intraregional effects: 
$$B^{LL}, B^{MM} \rightarrow O_j^{LL}, O_j^{MM}$$

Interregional effects:  $B^{ML}, B^{LM} \rightarrow O_j^{ML}, O_j^{LM}$ 

<u>National effects</u>:  $O_j^L = O_j^{LL} + O_j^{ML}$  e  $O_j^M = O_j^{MM} + O_j^{LM}$ 

<u>Sectoral effects</u>:  $O_{ij}^{L} = \alpha_{ij}^{LL} + \alpha_{ij}^{ML}$  e  $O_{ij}^{M} = \alpha_{ij}^{MM} + \alpha_{ij}^{LM}$ 

Multipliers vary not only across sectors but also across regions.

A small regional economy, with a modest representation of industry, may not be able to provide all the necessary inputs required by local industry. Thus, there will be considerable importation of inputs (sometimes referred to as leakages).

In general, the larger the value of the imports, the lower the value of the multiplier.

We would expect multipliers to decrease as we move from the country as a whole to a macro-region, an individual province, a metropolitan region and finally to a municipality.

## Mexican interregional input-output system, 2013





The University of São Paulo **Regional and Urban Economics Lab** 

#### Interregional Input-Output Tables for Mexico, 2013



Instituto de Investigaciones en Medio Ambiente Xavier Gorostiaga, S.J.





Reference: Haddad, E. A., Araújo, I. F., Ibarrarán, M. E., Boyd, R., Elizondo, A., Liedo, P., Belausteguigoitia, J. C., and Menchero, M. (2019). Interregional Input-Output System for Mexico, 2013, TD NEREUS 07-2019, The University of São Paulo Regional and Urban Economics Lab (NEREUS).

### http://www.scielo.org.mx/scielo.php?script=sci\_arttext&pid=S2448-66552020000300007

https://www.researchgate.net/publication/344121142 Interstate inputoutput model for Mexico 2013

## List of sectors

| Id          | Cod.<br>SUT* | Sectors  |
|-------------|--------------|--|
| <b>S</b> 1  | 111          | Agriculture  |
| S2          | 112          | Animal production  |
| <b>S</b> 3  | 113          | Forestry and logging   |
| S4          | 114          | Fishing and aquaculture  |
| <b>S</b> 5  | 115          | Agriculture, farming, forestry and fishing support service activities  |
| <b>S</b> 6  | 211          | Extraction of crude petroleum and natural gas  |
| <b>S</b> 7  | 212-213      | Mining and support service activities  |
| <b>S</b> 8  | 221          | Electric power generation, transmission and distribution   |
| <b>S</b> 9  | 222          | Water and gas supply by pipelines to the final consumer  |
| S10         | 236-238      | Construction   |
| S11         | 311          | Manufacture of food products   |
| S12         | 312          | Manufacture of beverages and tobacco products  |
| S13         | 313-314      | Manufacture of textiles  |
| S14         | 315-316      | Manufacture of wearing apparel   |
| S15         | 321          | Manufacture of wood and of products of wood and cork, except furniture   |
| <b>S</b> 16 | 322-323      | Manufacture of paper and paper products; Printing and reproduction of recorded media   |
| S17         | 324-326      | Manufacture of coke and refined petroleum products; Manufacture of chemicals<br>and chemical products; Manufacture of rubber and plastics products   |
| S18         | 327          | Manufacture of other non-metallic mineral products   |
| S19         | 331-332      | Manufacture of basic metals; Manufacture of fabricated metal products, except<br>machinery and equipment   |
| S20         | 333-336      | Manufacture of machinery and equipment n.e.c.; Manufacture of computer,<br>electronic and optical products; Manufacture of electrical equipment;<br>Manufacture of motor vehicles, trailers and semi-trailers; Manufacture of other<br>transport equipment |
| S21         | 337          | Manufacture of furniture   |
| S22         | 339          | Other manufacturing  |
| S23         | 431          | Wholesale trade  |
| S24         | 461          | Retail trade   |
| S25         | 481-493      | Transportation and storage   |
| S26         | 511-519      | Information and communication  |
| S27         | 521-524      | Financial and insurance activities   |
| S28         | 531-533      | Real estate activities   |
| S29         | 541          | Professional, scientific and technical activities  |
| S30         | 551          | Activities of head offices; management consultancy activities  |
| S31         | 561-562      | Administrative and support service activities  |
| S32         | 611          | Education  |
| S33         | 621-624      | Human health and social work activities  |
| <b>S</b> 34 | 711-713      | Arts, entertainment and recreation   |
| S35         | 721-722      | Accommodation and food service activities  |
| S36         | 811-814      | Other service activities   |
| <b>S</b> 37 | 931          | Public administration and defense; compulsory social security; Activities of<br>extraterritorial organizations and bodies  |

### Aggregate trade flows in Mexico

#### Annex 4.A. Interregional Trade in Mexico, 2013 (in MXN billions)

|     | DESTINATION TOT |     |      |     |     |      |     |     |      |      |     |      |     |     | OTAL |      |     |     |     |      |     |     |     |     |     |     |     |     |     |     |      |     |     |      |       |
|-----|-----------------|-----|------|-----|-----|------|-----|-----|------|------|-----|------|-----|-----|------|------|-----|-----|-----|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|-----|-----|------|-------|
|     | -               | R1  | R2   | R3  | R4  | R5   | R6  | R7  | R8   | R9   | R10 | R11  | R12 | R13 | R14  | R15  | R16 | R17 | R18 | R19  | R20 | R21 | R22 | R23 | R24 | R25 | R26 | R27 | R28 | R29 | R30  | R31 | R32 | ROW  | 0     |
|     | <b>R</b> 1      | 159 | 2    | 0   | 6   | 4    | 1   | 2   | 4    | 20   | 1   | 7    | 1   | 1   | 10   | 6    | 2   | 1   | 1   | 8    | 1   | 2   | 3   | 1   | 4   | 1   | 2   | 4   | 3   | 0   | 4    | 1   | 5   | 91   | 355   |
|     | R2              | 2   | 456  | 3   | 29  | 11   | 1   | 6   | 12   | 27   | 2   | 3    | 1   | 1   | 7    | 7    | 1   | 1   | 1   | 13   | 1   | 3   | 2   | 2   | 2   | 3   | 16  | 14  | 4   | 0   | 9    | 2   | 3   | 256  | 899   |
|     | R3              | 1   | 8    | 84  | 11  | 5    | 0   | 2   | 4    | 13   | 1   | 2    | 0   | 0   | 2    | 3    | 0   | 0   | 0   | 7    | 0   | 1   | 1   | 0   | 1   | 1   | 4   | 5   | 2   | 0   | 3    | 0   | 1   | 8    | 170   |
|     | R4              | 1   | 5    | 0   | 164 | 8    | 0   | 15  | 4    | 45   | 1   | 26   | 0   | 13  | 23   | 47   | 3   | 6   | 1   | 32   | 13  | 6   | 11  | 1   | 6   | 1   | 4   | 44  | 41  | 2   | 42   | 2   | 1   | 347  | 915   |
|     | R5              | 5   | 13   | 2   | 20  | 478  | 1   | 5   | 28   | 39   | 5   | 9    | 2   | 2   | 15   | 15   | 4   | 2   | 1   | 93   | 3   | 7   | 5   | 3   | 6   | 5   | 12  | 12  | 17  | 1   | 13   | 3   | 5   | 448  | 1279  |
|     | R6              | 1   | 2    | 0   | 5   | 3    | 73  | 1   | 2    | 12   | 0   | 2    | 0   | 0   | 6    | 3    | 1   | 0   | 0   | 4    | 0   | 1   | 1   | 0   | 1   | 0   | 2   | 3   | 1   | 0   | 2    | 0   | 1   | 8    | 139   |
|     | R7              | 2   | 8    | 1   | 16  | 7    | 1   | 233 | 7    | 39   | 2   | 5    | 2   | 2   | 7    | 11   | 2   | 1   | 1   | 13   | 2   | 5   | 3   | 3   | 2   | 2   | 6   | 20  | 5   | 1   | 13   | 4   | 1   | 33   | 462   |
|     | R8              | 3   | 13   | 1   | 18  | 21   | 1   | 5   | 416  | 32   | 5   | 6    | 1   | 1   | 11   | 11   | 3   | 2   | 1   | 29   | 2   | 5   | 3   | 2   | 4   | 4   | 14  | 11  | 8   | 1   | 10   | 2   | 4   | 330  | 979   |
|     | R9              | 22  | 46   | 6   | 59  | 58   | 6   | 21  | 59   | 2566 | 12  | 68   | 18  | 44  | 69   | 256  | 25  | 28  | 7   | 73   | 21  | 72  | 49  | 8   | 34  | 15  | 41  | 60  | 51  | 13  | 92   | 10  | 14  | 166  | 4088  |
|     | R10             | 2   | 5    | 1   | 8   | 12   | 0   | 2   | 11   | 20   | 148 | 4    | 1   | 1   | 7    | 7    | 2   | 1   | 1   | 18   | 1   | 2   | 2   | 1   | 3   | 3   | 5   | 5   | 5   | 0   | 5    | 1   | 3   | 31   | 317   |
| -   | R11             | 11  | 12   | 2   | 18  | 17   | 2   | 5   | 16   | 99   | 4   | 556  | 3   | 4   | 32   | 28   | 9   | 3   | 2   | 28   | 3   | 10  | 16  | 3   | 12  | 5   | 10  | 13  | 13  | 1   | 16   | 3   | 7   | 187  | 1151  |
| -   | R12             | 2   | 4    | 0   | 11  | 6    | 0   | 2   | 6    | 58   | 1   | 4    | 138 | 1   | 5    | 11   | 1   | 3   | 0   | 10   | 1   | 5   | 3   | 1   | 2   | 1   | 3   | 8   | 3   | 1   | 7    | 1   | 1   | 19   | 318   |
| -   | R13             | 2   | 4    | 1   | 7   | 5    | 1   | 2   | 5    | 101  | 1   | 6    | 2   | 179 | 7    | 18   | 2   | 2   | 1   | 8    | 1   | 9   | 5   | 1   | 3   | 1   | 3   | 6   | 4   | 2   | 10   | 1   | 1   | 33   | 435   |
| -   | R14             | 18  | 22   | 3   | 36  | 30   | 6   | 9   | 28   | 145  | 7   | 38   | 4   | 6   | 897  | 44   | 18  | 5   | 6   | 50   | 4   | 15  | 17  | 5   | 17  | 10  | 19  | 24  | 23  | 2   | 27   | 5   | 11  | 306  | 1855  |
|     | R15             | 9   | 17   | 3   | 26  | 24   | 3   | 8   | 22   | 659  | 5   | 27   | 8   | 13  | 34   | 1052 | 12  | 13  | 3   | 43   | 7   | 31  | 25  | 5   | 13  | 6   | 15  | 23  | 19  | 5   | 35   | 5   | 5   | 300  | 2475  |
| NI: | R16             | 5   | 8    | 1   | 10  | 12   | 1   | 2   | 10   | 63   | 2   | 14   | 1   | 3   | 30   | 21   | 246 | 2   | 1   | 18   | 2   | 6   | 8   | 1   | 5   | 2   | 7   | 8   | 7   | 1   | 10   | 2   | 2   | 51   | 562   |
| RIC | R17             | 1   | 2    | 0   | 5   | 3    | 0   | 1   | 3    | 51   | 1   | 3    | 2   | 1   | 4    | 11   | 1   | 157 | 0   | 5    | 1   | 5   | 2   | 1   | 1   | 1   | 2   | 4   | 2   | 1   | 5    | 1   | 1   | 62   | 338   |
| Ō   | R18             | 1   | 2    | 0   | 4   | 4    | 0   | 1   | 3    | 15   | 1   | 2    | 0   | 0   | 6    | 3    | 1   | 0   | 78  | 6    | 0   | 1   | 1   | 0   | 1   | 1   | 2   | 3   | 2   | 0   | 2    | 0   | 1   | 7    | 154   |
| -   | R19             | 11  | 29   | 4   | 44  | 118  | 3   | 11  | 52   | 89   | 9   | 20   | 4   | 4   | 30   | 27   | 7   | 4   | 3   | 1148 | 5   | 13  | 10  | 5   | 15  | 10  | 25  | 28  | 64  | 2   | 27   | 6   | 12  | 388  | 2226  |
|     | R20             | 2   | 6    | 1   | 18  | 7    | 1   | 5   | 6    | 51   | 1   | 5    | 1   | 2   | 6    | 11   | 2   | 2   | 1   | 12   | 189 | 8   | 3   | 2   | 2   | 2   | 5   | 12  | 4   | 1   | 13   | 2   | 2   | 27   | 409   |
|     | R21             | 4   | 7    | 1   | 21  | 9    | 1   | 7   | 9    | 149  | 2   | 11   | 3   | 8   | 14   | 36   | 4   | 7   | 1   | 17   | 6   | 428 | 8   | 3   | 5   | 2   | 6   | 18  | 7   | 7   | 36   | 3   | 2   | 164  | 1006  |
|     | R22             | 4   | 5    | 1   | 11  | 8    | 1   | 3   | 7    | 74   | 2   | 16   | 2   | 3   | 13   | 22   | 4   | 2   | 1   | 13   | 2   | 7   | 289 | 1   | 7   | 2   | 4   | 8   | 6   | 1   | 10   | 2   | 3   | 119  | 651   |
| -   | R23             | 1   | 6    | 0   | 33  | 8    | 0   | 2   | 8    | 35   | 1   | 4    | 0   | 1   | 3    | 6    | 1   | 1   | 0   | 14   | 1   | 3   | 2   | 144 | 2   | 1   | 5   | 12  | 6   | 0   | 6    | 3   | 1   | 10   | 320   |
|     | R24             | 7   | 5    | 1   | 10  | 11   | 1   | 3   | 8    | 46   | 2   | 13   | 1   | 2   | 16   | 14   | 3   | 2   | 1   | 22   | 2   | 5   | 8   | 1   | 272 | 2   | 4   | 7   | 10  | 1   | 9    | 1   | 6   | 113  | 611   |
| -   | R25             | 3   | 14   | 1   | 17  | 18   | 1   | 3   | 15   | 36   | 4   | 5    | 1   | 1   | 13   | 9    | 2   | 1   | 1   | 23   | 1   | 4   | 3   | 1   | 3   | 241 | 15  | 10  | 7   | 1   | 8    | 2   | 3   | 34   | 500   |
|     | R26             | 3   | 33   | 3   | 33  | 19   | 2   | 8   | 23   | 42   | 3   | 8    | 2   | 2   | 17   | 16   | 5   | 3   | 2   | 27   | 3   | 7   | 4   | 3   | 4   | 9   | 458 | 18  | 7   | 1   | 18   | 4   | 4   | 244  | 1035  |
| -   | R27             | 3   | 13   | 2   | 33  | 11   | 1   | 18  | 11   | 56   | 3   | 18   | 3   | 9   | 18   | 34   | 5   | 4   | 1   | 25   | 9   | 10  | 8   | 6   | 6   | 5   | 11  | 303 | 23  | 2   | 40   | 9   | 2   | 177  | 878   |
|     | R28             | 5   | 13   | 2   | 23  | 26   | 2   | 5   | 18   | 51   | 4   | 11   | 2   | 3   | 15   | 16   | 4   | 2   | 1   | 66   | 2   | 6   | 6   | 2   | 9   | 5   | 11  | 13  | 404 | 1   | 14   | 3   | 6   | 230  | 980   |
|     | R29             | 1   | 1    | 0   | 3   | 2    | 0   | 1   | 2    | 26   | 0   | 2    | 0   | 1   | 2    | 6    | 1   | 1   | 0   | 3    | 1   | 9   | 2   | 0   | 1   | 0   | 1   | 2   | 1   | 69  | 5    | 1   | 0   | 20   | 164   |
| -   | R30             | 6   | 17   | 3   | 30  | 18   | 2   | 11  | 18   | 149  | 4   | 18   | 6   | 10  | 24   | 44   | 7   | 6   | 2   | 33   | 8   | 31  | 11  | 6   | 8   | 6   | 15  | 31  | 17  | 5   | 706  | 7   | 4   | 142  | 1404  |
|     | R31             | 1   | 4    | 0   | 35  | 4    | 0   | 3   | 4    | 18   | 1   | 2    | 1   | 1   | 4    | 5    | 1   | 1   | 0   | 7    | 1   | 2   | 1   | 5   | 1   | 1   | 3   | 15  | 3   | 0   | 6    | 186 | 1   | 22   | 341   |
|     | R32             | 4   | 2    | 0   | 5   | 6    | 0   | 1   | 4    | 16   | 1   | 5    | 0   | 1   | 6    | 5    | 2   | 1   | 0   | 12   | 0   | 2   | 2   | 0   | 4   | 1   | 2   | 3   | 3   | 0   | 5    | 1   | 100 | 33   | 228   |
|     | ROW             | 96  | 215  | 16  | 139 | 369  | 15  | 73  | 269  | 603  | 37  | 229  | 26  | 70  | 330  | 450  | 60  | 66  | 15  | 492  | 51  | 233 | 146 | 26  | 133 | 48  | 247 | 153 | 226 | 29  | 230  | 38  | 37  | 0    | 5167  |
| TO  | TAL             | 398 | 1000 | 143 | 907 | 1341 | 128 | 477 | 1092 | 5445 | 274 | 1148 | 235 | 391 | 1678 | 2256 | 439 | 328 | 133 | 2372 | 343 | 955 | 661 | 245 | 590 | 394 | 979 | 902 | 999 | 150 | 1440 | 311 | 250 | 4407 | 32809 |

The conventional input-output model is given by the system of matrix equations:

 $x = (I - A)^{-1}f = Bf$ 

where x and f are respectively the vectors of gross output and final demand; A consists of input coefficients  $a_{ij}$  defined as the amount of product *i* required per unit of product *j* (in monetary terms), for *i*, *j* = 1,..., n; and *B* is known as the Leontief inverse. In an interregional context, with *R* different regions, we have:

$$x = \begin{bmatrix} x^1 \\ \vdots \\ x^R \end{bmatrix}; A = \begin{bmatrix} A^{11} & \cdots & A^{1R} \\ \vdots & \ddots & \vdots \\ A^{R1} & \cdots & A^{RR} \end{bmatrix}; f = \begin{bmatrix} f^1 \\ \vdots \\ f^R \end{bmatrix}; \text{ and } B = \begin{bmatrix} B^{11} & \cdots & B^{1R} \\ \vdots & \ddots & \vdots \\ B^{R1} & \cdots & B^{RR} \end{bmatrix}$$

and

$$x^{1} = B^{11}f^{1} + \dots + B^{1R}f^{R}$$
  

$$\vdots$$
  

$$x^{R} = B^{R1}f^{1} + \dots + B^{RR}f^{R}$$

Let us also consider different components of f, which include demands originating in the specific regions,  $v^{rs}$ , s = 1,..., R, and abroad, e. We obtain information of final demand from origin s in the IIOM-MEX, allowing us to treat v as a matrix which provides the monetary values of final demand expenditures from the domestic regions in Mexico and from the foreign region.

$$v = \begin{bmatrix} v^{11} & \cdots & v^{1R} \\ \vdots & \ddots & \vdots \\ v^{R1} & \cdots & v^{RR} \end{bmatrix}; \ e = \begin{bmatrix} e^1 \\ \vdots \\ e^R \end{bmatrix}$$

Thus:

$$\begin{aligned} x^{1} &= B^{11}(v^{11} + \dots + v^{R1} + e^{1}) + \dots + B^{1R}(v^{1R} + \dots + v^{RR} + e^{R}) \\ &\vdots \\ x^{R} &= B^{R1}(v^{11} + \dots + v^{R1} + e^{1}) + \dots + B^{RR}(v^{1R} + \dots + v^{RR} + e^{R}) \end{aligned}$$

## Spatial propagation of final demand shocks (...)

Table 2. Components of Decomposition of Regional Output Based on the Sources of Final Demand: Mexico, 2013 (in %)

|    | _          | ORIGIN OF FINAL DEMAND |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |
|----|------------|------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|    |            | R1                     | R2    | R3    | R4    | R5    | R6    | R7    | R8    | R9    | R10   | R11   | R12   | R13   | R14   | R15   | R16   | R17   | R18   | R19   | R20   | R21   | R22   | R23   | R24   | R25   | R26   | R27   | R28   | R29   | R30   | R31   | R32 1 | ROW   |
|    | R1         | 34.43                  | 0.65  | 0.09  | 1.86  | 0.94  | 0.14  | 0.45  | 0.97  | 6.43  | 0.22  | 1.31  | 0.12  | 0.17  | 1.71  | 1.18  | 0.34  | 0.15  | 0.13  | 1.98  | 0.17  | 0.45  | 0.53  | 0.17  | 0.70  | 0.22  | 0.40  | 1.18  | 0.80  | 0.06  | 1.09  | 0.16  | 1.06  | 39.75 |
|    | R2         | 0.17                   | 39.09 | 0.22  | 3.57  | 0.96  | 0.06  | 0.67  | 1.12  | 3.43  | 0.12  | 0.31  | 0.06  | 0.07  | 0.48  | 0.58  | 0.12  | 0.08  | 0.06  | 1.26  | 0.09  | 0.32  | 0.17  | 0.14  | 0.18  | 0.21  | 1.12  | 1.65  | 0.42  | 0.03  | 0.93  | 0.13  | 0.33  | 41.84 |
|    | R3         | 0.46                   | 4.78  | 39.70 | 7.88  | 2.70  | 0.08  | 1.38  | 2.39  | 9.69  | 0.38  | 0.92  | 0.10  | 0.22  | 1.04  | 1.63  | 0.22  | 0.17  | 0.09  | 3.96  | 0.16  | 0.83  | 0.50  | 0.17  | 0.50  | 0.31  | 1.81  | 3.72  | 1.23  | 0.09  | 2.13  | 0.24  | 0.65  | 9.87  |
|    | R4         | 0.45                   | 1.04  | 0.18  | 18.52 | 1.25  | 0.18  | 0.84  | 1.11  | 8.28  | 0.26  | 1.01  | 0.24  | 0.25  | 1.46  | 1.93  | 0.43  | 0.30  | 0.16  | 2.42  | 0.26  | 0.84  | 0.58  | 0.40  | 0.53  | 0.45  | 0.87  | 2.47  | 0.70  | 0.12  | 1.74  | 0.48  | 0.43  | 49.83 |
|    | R5         | 0.23                   | 0.75  | 0.11  | 1.75  | 23.40 | 0.08  | 0.40  | 1.29  | 3.54  | 0.23  | 0.45  | 0.09  | 0.09  | 0.66  | 0.71  | 0.17  | 0.11  | 0.09  | 4.26  | 0.13  | 0.30  | 0.23  | 0.17  | 0.26  | 0.27  | 0.48  | 1.01  | 0.85  | 0.04  | 0.80  | 0.15  | 0.30  | 56.59 |
|    | R6         | 0.77                   | 1.46  | 0.10  | 4.30  | 1.70  | 44.73 | 0.85  | 1.82  | 10.76 | 0.24  | 1.32  | 0.14  | 0.24  | 3.29  | 1.96  | 0.45  | 0.24  | 0.19  | 2.93  | 0.19  | 0.79  | 0.67  | 0.20  | 0.65  | 0.30  | 1.07  | 2.49  | 1.06  | 0.10  | 1.73  | 0.26  | 0.73  | 12.29 |
|    | R7         | 0.45                   | 1.80  | 0.25  | 4.03  | 1.52  | 0.16  | 40.04 | 1.69  | 11.79 | 0.32  | 1.03  | 0.30  | 0.33  | 1.40  | 2.00  | 0.41  | 0.30  | 0.16  | 3.11  | 0.37  | 1.02  | 0.67  | 0.71  | 0.49  | 0.47  | 1.13  | 4.04  | 1.08  | 0.14  | 2.17  | 0.79  | 0.28  | 15.54 |
|    | <b>R</b> 8 | 0.23                   | 1.10  | 0.10  | 1.97  | 1.33  | 0.07  | 0.43  | 31.77 | 3.68  | 0.22  | 0.45  | 0.08  | 0.09  | 0.65  | 0.70  | 0.16  | 0.10  | 0.08  | 2.18  | 0.12  | 0.31  | 0.23  | 0.15  | 0.24  | 0.25  | 0.80  | 1.09  | 0.60  | 0.04  | 0.82  | 0.15  | 0.33  | 49.45 |
|    | R9         | 0.56                   | 1.28  | 0.14  | 1.75  | 1.34  | 0.14  | 0.56  | 1.50  | 58.06 | 0.29  | 1.54  | 0.33  | 0.84  | 1.53  | 4.97  | 0.51  | 0.58  | 0.16  | 2.06  | 0.44  | 1.48  | 1.07  | 0.22  | 0.73  | 0.33  | 0.88  | 1.58  | 1.21  | 0.26  | 2.17  | 0.29  | 0.33  | 10.86 |
|    | R10        | 0.71                   | 1.86  | 0.23  | 3.44  | 3.10  | 0.15  | 0.76  | 3.33  | 9.65  | 34.10 | 1.28  | 0.18  | 0.26  | 1.85  | 1.91  | 0.38  | 0.26  | 0.21  | 5.54  | 0.24  | 0.79  | 0.64  | 0.31  | 0.73  | 0.68  | 1.27  | 2.06  | 1.59  | 0.10  | 1.70  | 0.30  | 0.99  | 19.40 |
|    | R11        | 0.80                   | 1.04  | 0.15  | 2.12  | 1.19  | 0.18  | 0.52  | 1.32  | 10.96 | 0.27  | 35.69 | 0.20  | 0.29  | 2.11  | 1.99  | 0.60  | 0.24  | 0.17  | 2.42  | 0.22  | 0.76  | 1.10  | 0.24  | 0.82  | 0.36  | 0.71  | 1.42  | 1.08  | 0.10  | 1.41  | 0.24  | 0.58  | 28.70 |
|    | R12        | 0.56                   | 1.49  | 0.09  | 4.22  | 1.78  | 0.09  | 0.83  | 1.85  | 20.99 | 0.21  | 1.17  | 35.14 | 0.40  | 1.46  | 2.97  | 0.30  | 0.69  | 0.10  | 3.19  | 0.26  | 1.34  | 0.84  | 0.21  | 0.57  | 0.20  | 0.96  | 2.89  | 1.15  | 0.16  | 2.26  | 0.33  | 0.42  | 10.90 |
| 5  | R13        | 0.45                   | 0.98  | 0.14  | 2.56  | 1.03  | 0.15  | 0.67  | 1.13  | 26.85 | 0.23  | 1.17  | 0.29  | 29.01 | 1.44  | 3.34  | 0.45  | 0.41  | 0.13  | 2.03  | 0.31  | 1.66  | 0.90  | 0.28  | 0.53  | 0.33  | 0.68  | 1.84  | 0.82  | 0.25  | 2.26  | 0.31  | 0.37  | 17.01 |
| Η  | R14        | 0.87                   | 1.32  | 0.17  | 2.45  | 1.45  | 0.29  | 0.56  | 1.62  | 10.38 | 0.31  | 1.81  | 0.18  | 0.29  | 35.19 | 2.06  | 0.80  | 0.25  | 0.29  | 2.92  | 0.23  | 0.77  | 0.84  | 0.26  | 0.78  | 0.44  | 0.89  | 1.60  | 1.32  | 0.10  | 1.50  | 0.26  | 0.59  | 27.21 |
| D  | R15        | 0.36                   | 0.80  | 0.11  | 1.53  | 0.89  | 0.12  | 0.41  | 0.94  | 28.16 | 0.18  | 1.02  | 0.26  | 0.43  | 1.20  | 32.08 | 0.41  | 0.44  | 0.11  | 1.85  | 0.26  | 0.98  | 0.85  | 0.22  | 0.44  | 0.25  | 0.54  | 1.20  | 0.79  | 0.15  | 1.46  | 0.23  | 0.23  | 21.13 |
| F  | R16        | 0.83                   | 1.42  | 0.14  | 2.69  | 1.71  | 0.19  | 0.55  | 1.78  | 14.69 | 0.26  | 2.02  | 0.20  | 0.37  | 3.53  | 2.75  | 33.48 | 0.32  | 0.21  | 3.36  | 0.25  | 0.92  | 1.16  | 0.25  | 0.72  | 0.33  | 0.95  | 1.85  | 1.32  | 0.13  | 1.70  | 0.29  | 0.47  | 19.13 |
| N  | R17        | 0.30                   | 0.70  | 0.09  | 2.13  | 0.80  | 0.09  | 0.52  | 0.79  | 16.84 | 0.15  | 0.71  | 0.34  | 0.29  | 0.88  | 2.44  | 0.26  | 35.79 | 0.08  | 1.49  | 0.21  | 1.11  | 0.53  | 0.17  | 0.34  | 0.20  | 0.48  | 1.47  | 0.58  | 0.13  | 1.53  | 0.19  | 0.26  | 28.10 |
| OE | R18        | 0.78                   | 1.66  | 0.13  | 3.74  | 2.41  | 0.17  | 0.75  | 2.28  | 12.43 | 0.49  | 1.61  | 0.14  | 0.30  | 3.10  | 2.13  | 0.47  | 0.22  | 42.66 | 4.18  | 0.18  | 0.84  | 0.87  | 0.19  | 0.70  | 0.44  | 1.31  | 2.17  | 1.42  | 0.10  | 1.72  | 0.22  | 0.61  | 9.54  |
| ξ  | R19        | 0.38                   | 1.15  | 0.15  | 2.59  | 3.33  | 0.12  | 0.59  | 1.84  | 5.30  | 0.32  | 0.70  | 0.14  | 0.13  | 1.00  | 0.99  | 0.26  | 0.15  | 0.11  | 38.21 | 0.18  | 0.46  | 0.35  | 0.22  | 0.45  | 0.36  | 0.75  | 1.51  | 1.93  | 0.05  | 1.22  | 0.23  | 0.54  | 34.28 |
| -  | R20        | 0.49                   | 1.50  | 0.18  | 5.49  | 1.66  | 0.14  | 1.30  | 1.59  | 15.94 | 0.27  | 1.11  | 0.28  | 0.38  | 1.35  | 2.39  | 0.39  | 0.36  | 0.13  | 3.09  | 34.82 | 1.76  | 0.77  | 0.38  | 0.52  | 0.38  | 0.97  | 3.56  | 1.06  | 0.19  | 3.07  | 0.44  | 0.44  | 13.59 |
|    | R21        | 0.32                   | 0.74  | 0.12  | 2.70  | 0.78  | 0.12  | 0.78  | 0.85  | 16.40 | 0.16  | 0.90  | 0.27  | 0.48  | 1.10  | 2.41  | 0.36  | 0.46  | 0.12  | 1.70  | 0.46  | 30.69 | 0.63  | 0.29  | 0.38  | 0.24  | 0.48  | 2.13  | 0.68  | 0.39  | 3.20  | 0.30  | 0.27  | 29.06 |
|    | R22        | 0.53                   | 0.77  | 0.12  | 2.25  | 1.00  | 0.14  | 0.58  | 1.01  | 13.30 | 0.21  | 1.77  | 0.20  | 0.33  | 1.51  | 2.44  | 0.49  | 0.27  | 0.13  | 1.95  | 0.24  | 0.82  | 31.28 | 0.22  | 0.72  | 0.28  | 0.54  | 1.54  | 0.89  | 0.11  | 1.59  | 0.24  | 0.44  | 32.10 |
|    | R23        | 0.51                   | 1.87  | 0.08  | 11.15 | 2.37  | 0.07  | 0.77  | 2.60  | 12.97 | 0.41  | 1.31  | 0.12  | 0.40  | 1.00  | 2.07  | 0.24  | 0.19  | 0.07  | 4.91  | 0.24  | 0.98  | 0.80  | 35.59 | 0.61  | 0.21  | 1.34  | 3.88  | 1.85  | 0.14  | 2.16  | 1.11  | 0.23  | 7.73  |
|    | R24        | 0.83                   | 0.84  | 0.13  | 2.36  | 1.36  | 0.16  | 0.58  | 1.21  | 9.17  | 0.27  | 1.59  | 0.17  | 0.23  | 1.74  | 1.71  | 0.41  | 0.22  | 0.15  | 3.14  | 0.22  | 0.64  | 0.88  | 0.23  | 31.63 | 0.30  | 0.54  | 1.52  | 1.34  | 0.08  | 1.44  | 0.22  | 0.84  | 33.83 |
|    | R25        | 0.58                   | 3.07  | 0.27  | 4.29  | 3.08  | 0.15  | 0.81  | 3.10  | 9.90  | 0.54  | 1.12  | 0.16  | 0.25  | 2.02  | 1.75  | 0.36  | 0.23  | 0.23  | 4.91  | 0.22  | 0.77  | 0.64  | 0.30  | 0.58  | 38.34 | 2.52  | 2.43  | 1.50  | 0.10  | 1.72  | 0.32  | 0.62  | 13.10 |
|    | R26        | 0.26                   | 2.48  | 0.27  | 3.66  | 1.09  | 0.14  | 0.79  | 1.69  | 5.20  | 0.23  | 0.60  | 0.14  | 0.13  | 1.06  | 1.07  | 0.28  | 0.16  | 0.16  | 1.98  | 0.20  | 0.48  | 0.30  | 0.30  | 0.28  | 0.66  | 29.26 | 1.93  | 0.63  | 0.06  | 1.43  | 0.27  | 0.38  | 42.45 |
|    | R27        | 0.48                   | 1.64  | 0.27  | 4.85  | 1.38  | 0.21  | 1.19  | 1.53  | 10.06 | 0.37  | 1.07  | 0.35  | 0.31  | 1.58  | 2.09  | 0.51  | 0.32  | 0.18  | 2.57  | 0.33  | 1.10  | 0.63  | 0.70  | 0.56  | 0.62  | 1.18  | 26.21 | 0.83  | 0.15  | 2.21  | 0.99  | 0.40  | 33.15 |
|    | R28        | 0.44                   | 1.25  | 0.16  | 2.78  | 2.08  | 0.14  | 0.59  | 1.59  | 6.83  | 0.31  | 0.82  | 0.17  | 0.16  | 1.18  | 1.23  | 0.32  | 0.16  | 0.13  | 5.06  | 0.16  | 0.57  | 0.44  | 0.23  | 0.61  | 0.40  | 0.82  | 1.55  | 29.12 | 0.07  | 1.28  | 0.26  | 0.56  | 38.52 |
|    | R29        | 0.37                   | 0.88  | 0.12  | 2.38  | 0.90  | 0.12  | 0.68  | 1.03  | 18.46 | 0.18  | 0.98  | 0.26  | 0.59  | 1.21  | 2.63  | 0.36  | 0.41  | 0.12  | 1.95  | 0.42  | 3.18  | 0.74  | 0.29  | 0.42  | 0.25  | 0.59  | 1.95  | 0.78  | 30.69 | 2.78  | 0.33  | 0.28  | 23.65 |
|    | R30        | 0.44                   | 1.35  | 0.19  | 2.80  | 1.20  | 0.15  | 0.78  | 1.40  | 13.97 | 0.27  | 1.07  | 0.32  | 0.43  | 1.45  | 2.39  | 0.43  | 0.37  | 0.15  | 2.48  | 0.40  | 1.65  | 0.71  | 0.43  | 0.51  | 0.41  | 0.88  | 2.36  | 1.00  | 0.22  | 39.29 | 0.48  | 0.32  | 19.73 |
|    | R31        | 0.30                   | 1.31  | 0.16  | 12.47 | 1.22  | 0.09  | 1.13  | 1.30  | 7.73  | 0.19  | 0.74  | 0.17  | 0.23  | 0.98  | 1.38  | 0.25  | 0.21  | 0.10  | 2.45  | 0.29  | 0.71  | 0.45  | 1.46  | 0.36  | 0.26  | 0.73  | 5.17  | 0.99  | 0.10  | 1.83  | 44.08 | 0.24  | 10.93 |
|    | R32        | 1.32                   | 1.00  | 0.12  | 2.54  | 1.74  | 0.14  | 0.60  | 1.62  | 8.78  | 0.38  | 1.45  | 0.16  | 0.23  | 1.79  | 1.72  | 0.38  | 0.24  | 0.14  | 3.86  | 0.19  | 0.73  | 0.72  | 0.22  | 1.03  | 0.29  | 0.66  | 1.55  | 1.16  | 0.09  | 1.52  | 0.23  | 36.23 | 27.17 |
| TO | FAL        | 0.92                   | 2.49  | 0.40  | 3.35  | 2.53  | 0.37  | 1.30  | 2.54  | 18.55 | 0.65  | 2.54  | 0.62  | 0.80  | 3.63  | 4.91  | 1.08  | 0.74  | 0.38  | 5.50  | 0.78  | 2.00  | 1.41  | 0.70  | 1.23  | 1.04  | 1.88  | 2.58  | 2.06  | 0.32  | 3.58  | 0.85  | 0.71  | 27.55 |

## Figure 3. Identification of Regions Relatively More Affected by a Specific Regional Demand, by Origin of Final Demand (cont.)

Rest of the World





## Spatial propagation of final demand shocks (...)



## Spatial propagation of final demand shocks



Input-output applications

 Mexican regions (how do they relate?), structural decomposition analysis (historical estimation, updating), main drivers of sectoral and regional growth, impact of interregional government transfers, impact analysis...

Interregional CGE applications

 Economic impacts of drought, regional impacts of climate change (agriculture), specific transportation projects (accessibility), simulate TFP-enhancing policies (sectors and regions), other usual CGE applications, ...

# **Exercise** – Interregional IO (decomposition of multiplier effects)

## <u>Data</u>: Mexican 32-region interregional input-output table, 2013

### 1. Agriculture (S1) in Sinaloa (R25)

2. Mexican exports and KIBS

Excel files (...)



### Interregional CGE Model for Mexico

Results

GRunGEM - BMMX <u>File Copy View Options H</u>elp Picture Text Model/Data Closure Shocks Output files Solve – Ø ×

**BM-MX Model** 

### Interregional Computable General Equilibrium Model for Mexico



The University of Sao Paulo Regional and Urban Economics Lab - NEREUS

May 2019

# BMMX ICGE, a bottom-up spatial CGE model of Mexico

A multi-sectoral, multi-regional bottom-up CGE model of Mexico's 32 regions

- each region is modeled as an economy in its own right
- region-specific prices
- region-specific industries
- region-specific consumers

Based on the comparative-static B-MARIA and MMRF models

Database makes allowance for interregional, intra-regional and international trade

 Potential for the representation of regional and Federal government financial accounts

## Stylized flows



## Core database

|                |           |           |   | ABSORPTION N | <b>/</b> ATRIX |                   |               |  |  |  |  |
|----------------|-----------|-----------|---|--------------|----------------|-------------------|---------------|--|--|--|--|
|                |           | 1         | 2   | 3            | 4              | 5                 | 6             |  |  |  |  |
|                |           | Producers | Investors   | Household    | Export         | Regional<br>Govt. | Federal Govt. |  |  |  |  |
|                | Size      | J x Q     | J x Q   | Q            | 1              | Q                 | Q             |  |  |  |  |
| Basic<br>Flows | I x S     | BAS1      | BAS2  | BAS3         | BAS4           | BAS5              | BAS6          |  |  |  |  |
| Margins        | I x S x R | MAR1      | MAR2  | MAR3         | MAR4           | MAR5              | MAR6          |  |  |  |  |
| Taxes          | I x S     | TAX1      | TAX2  | TAX3         | TAX4           | TAX5              | TAX6          |  |  |  |  |
| Labor          | 1         | LABR      |   | 8            |                |                   | 8             |  |  |  |  |
| Capital        | 1         | CPTL      | I = number of co  |              |                |                   |               |  |  |  |  |
| Other          | 1         | OCTS      | $\begin{array}{c} \textbf{OCTS} \\ J = number of industries \\ \textbf{D} \\ \end{array}$ |              |                |                   |               |  |  |  |  |

R = number of commodities used as margins

Q = number of regions

S = Q domestic regions + 1 foreign import

Commodity flows are valued at "basic prices" (BAS):

do not include user-specific taxes or margins

For each user of each imported good and each domestic good, there are numbers showing:

- tax levied on that usage (TAX)
- usage of margins transport (MAR)\*

Single-production:

- each commodity may be produced by one industry
- each industry may produce one commodity

For each industry the total cost of production is equal to the total value of output

For each commodity the total value of sales is equal to the total value of output

Domestic producers

J industries in Q regions

Investors

J industries in Q regions

Households

one representative household for each of the Q regions

Each of the I commodity types can be obtained from the region, from other regions, or imported from overseas

Aggregate foreign purchaser of exports

Other demand category corresponding to the Q regional governments

Other demand category corresponding to the central government in the Q regions

Commodity taxes and margins explicitly recognised

## **Building blocks**

### ✓ Producer's demands for inputs

- Investor demands
- Household demands
- Export demands
- Government demands
- Margins demands
- ✓ Zero pure profits
- Indirect tax equations
- Market-clearing
- Regional and national macroeconomic variables and price indexes
- Capital accumulation and investment
- Regional population and labor market

## **Production nest**



## Investment demand



## Household demand



## Foreign export demand



Export commodities face individual downward-sloping foreign export demand functions

Exports of product i from source s are distinguished from exports of i from source r (r not equal s) Recognise regional governments and Federal government demands for goods and services for current consumption (not properly calibrated yet!)

Neither modelled explicitly

Default:

- aggregate regional government demand in region q moves with regional government revenue, with structure of demand exogenous
- aggregate Federal government demand in region q moves with national government revenue, with structure of demand exogenous

Margins commodities (identified in the set MARGCOM) provide freight services

- these commodities are consumed directly and used indirectly to facilitate the movements of products
- latter type of use is margins demand

Margins demand for margin commodity i is assumed to be proportional to the volume of the underlying flow

 e.g., margins use of transportation services in taking agricultural products to manufacturing is modelled as proportional to the volume of agricultural product used in manufacturing Critical assumptions

- no pure profits in the production or distribution of commodities
- price received by the producer is uniform across all customers

Zero pure profits in current production imposed by setting unit prices received by producers equal to unit costs

Zero pure profits in distribution imposed by setting the prices paid by users equal to producer price plus commodity tax plus margins Equations have been added to enable flexible handling of indirect taxes on all flows of goods and services

Equations allow for variations in tax rates across commodities, their sources and destinations

Equations that impose market clearing (demand equals supply) for:

- domestically produced margin and non-margin commodities
- imported commodities

Wide range of national and regional macro variables defined...

Two concepts of the real wage rate

- consumer real wage rate (PLAB/CPI)
- producer real wage rate (PLAB/PGDP)

Capital, investment and expected rates of return

$$K_{j,q}(t+1) = (1 - DEP_{j,q}) \times K_{j,q}(t) + Y_{j,q}(t)$$

Given starting point for capital (t=0) and an explanation of investment, we can trace out time path for capital

Investment explained by assuming that:

$$\frac{K_{j,q}(t+1)}{K_{j,q}(t)} - 1 = F_{j,q}^{t} [EROR_{j,q}(t)]$$

Growth in capital related to expected rate of return

 In BMMX ICGE only assume static expectations, though rational is possible For static expectations case, the actual rate of return is:

$$RO_t(j,q) = \frac{P_t(j,q)}{\prod_t(j,q)} - D(j,q)$$

 $ro(j,q) = p_t(j,q) - \pi_t(j,q)$ 

 $ro(j,q) = QCOEF(j,q) [p_t(j,q) - \pi_t(j,q)]$ 

QCOEF: relação entre taxa bruta e taxa líquida de retorno (> 1)

In long-run comparative-static simulations:

- aggregate capital adjusts to maintain R<sub>INT</sub> (natr\_tot)
- capital allocated in line with equation E\_f\_rate\_xx
  - industries with relatively large increases in capital require relatively high rates of return
  - industries with relatively small increases in capital require relatively low rates of return
- industry investment determined by fixed ratios of investment to capital (equation E\_y)

### Equalization in the rates of return

$$\left(\frac{K(j,q)}{K(q)}\right)^{-\beta(j,q)} RO(j,q) = R_{\text{int}}$$

$$ro(j,q) - r_{int} = \beta_t(j,q) [k(j,q) - k(q)] + f_rate(j,q)$$

### beta: risk/return ratio

Short-run: *f\_rate* endogenous, *k* exogenous

Long-run: *f\_rate* exogenous, *k* endogenous

Growth rate of capital stocks and investment in the short-run:

 $k_{t+1}(j,q) - k_t(j,q) = 0$ 

% change in capital stocks

 $y_t(j,q) = 0$ 

% change in investment

Growth rate of capital stocks and investment in the long-run:

$$\frac{K_{j,q}(t+1)}{K_{j,q}(t)} = \left(\frac{K_{j,q}(t)}{K_{j,q}(0)}\right)^{1/T}$$

$$k_{t+1}(j,q) = \left(1 + \frac{1}{T}\right)k_t(j,q)$$

Fixed capital stocks in the base year values:

- curcap(j,q) exogenous (=0)
- relationship between sectoral rates of return, r0(j,q), and reference interest rate, natr\_tot, is endogenous (f\_rate\_xx(j,q) endogenous)

Percentage change in sectoral investment, y(j,q) is zero; this can be guaranteed by setting the shift term,  $delf_rate(j,q)$ , exogenous and zero

By hypothesis, not only the capital stocks are fixed but also firms' investment plans

Capital stocks endogenously determined:

- curcap(j,q) endogenous
- relationship between sectoral rates of return,, r0(j,q), and reference interest rate, natr\_tot, is given (f\_rate\_xx(j,q) exogenous)

Percentage change in sectoral investment, y(j,q) is endogenous

Firms' investment plans are carried out, reestablishing returns differentials in the base year

Rate of capital accumulation, but **not the level** of capital stock, remains constant

## Regional population and labor market

Critical variables:

- regional population
- regional migration
- regional unemployment
- regional participation rates
- regional wage relativities

Various closures

## Regional population and labor market

(1) Fixed

- wage relativities (determining employment by region), participation and unemployment rates (determining population by region)
- (1) Endogenous
  - regional migration
- (2) Fixed
  - regional migration, participation rates, wage relativities

### (2) Endogenous

### unemployment rates

- (3) Fixed
  - regional migration, participation and unemployment rates
- (3) Endogenous
  - wage relativities



Each equation explains a variable

More variables than equations

Endogenous variables: explained by model

Exogenous variables: set by user

Closure: choice of exogenous variables

Many possible closures

Number of endogenous variables = Number of equations

# **Exercise** – CGE model (simulating the short-run effects of a drought in Northern Mexico)

 Most years, one or more regions of Mexico suffer from low rainfall. As a continuing result of climate change, during 2020 an unusually severe drought in Sinaloa is expected to affect farmers all over the region. Agricultural outputs will fall sharply, with an expected loss of 10% (what if climate variability would also affect cattle raising output?). We will simulate the effects of such a drought using the BMMX ICGE model.

*Guide for the BMMX Interregional CGE Model for Mexico Using Customized RunGEM* 

GEMPACK...

## **Production nest**





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